

15.4 Matrix Review and Matrix Transformations



Give the dimensions of each matrix. (rowXcolumn)

1. $\begin{bmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \end{bmatrix}$	2. $\begin{bmatrix} 0 & 4 & 8 \\ 1 & 5 & 9 \\ 2 & 6 & 0 \\ 3 & 7 & 1 \end{bmatrix}$	3. $\begin{bmatrix} 5 & -5 \\ 2 & 3 \\ 9 & 8 \end{bmatrix}$
4. $\begin{bmatrix} 4 & -1 \\ 0 & 2 \end{bmatrix}$	5. $\begin{bmatrix} 4 & 1 & -2 \\ 3 & -1 & 1 \end{bmatrix}$	6. $\begin{bmatrix} 5 \\ 8 \\ 2 \end{bmatrix}$
<p>7. If <math>AB</math> can be multiplied but <math>BA</math> CAN'T be multiplied, then <math>\longrightarrow</math> The _____ of the first matrix and the _____ of the second matrix must be the same.</p> <p><math>A = \begin{bmatrix} 3 &amp; 5 \end{bmatrix}</math>   <math>B = \begin{bmatrix} 4 &amp; 1 &amp; -2 \\ 3 &amp; -1 &amp; 1 \end{bmatrix}</math></p>		
8. In the expression $A \cdot B$ , if $A$ is a $3 \times 5$ matrix then what could be the dimensions of $B$ ?	9. In the expression $A \cdot B$ , if $A$ is a $1 \times 8$ matrix then what could be the dimensions of $B$ ?	10. In the expression $A \cdot B$ , if $B$ is a $2 \times 4$ matrix then what could be the dimensions of $A$ ?

11. Matrix Multiplication: Multiply \_\_\_\_\_ of the first matrix by \_\_\_\_\_ of the second matrix. Multiply corresponding part and then find the sum.

$$\begin{bmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \end{bmatrix} \times \begin{bmatrix} 7 & 8 \\ 9 & 10 \\ 11 & 12 \end{bmatrix} = \begin{bmatrix} 58 & 64 \\ 139 & 154 \end{bmatrix}$$

Find the product.

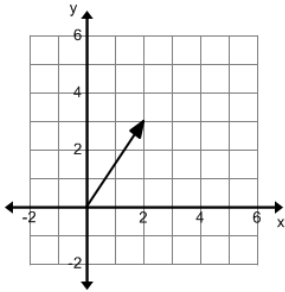
12. $\begin{bmatrix} -5 \\ 6 \\ 0 \end{bmatrix} \cdot \begin{bmatrix} 3 & -1 \end{bmatrix}$	13. $\begin{bmatrix} -5 & -5 \\ -1 & 2 \end{bmatrix} \cdot \begin{bmatrix} -2 & -3 \\ 3 & 5 \end{bmatrix}$	14. $\begin{bmatrix} 2 \\ 6 \end{bmatrix} \cdot \begin{bmatrix} -2 & 3 \\ 4 & 7 \end{bmatrix}$
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15. You start up a baking business and sell cupcakes for \$3, pies for \$4, and cookies for \$2. You use a matrix to keep track of how much you sell in a week. The first column is Monday and goes through Thursday. How much money did you make?

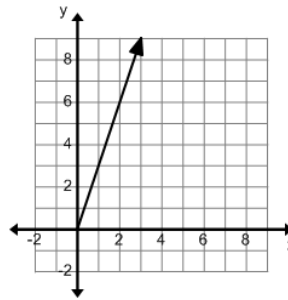
$$\begin{bmatrix} \$3 & \$4 & \$2 \end{bmatrix} \cdot \begin{bmatrix} 13 & 9 & 7 & 15 \\ 8 & 7 & 4 & 6 \\ 6 & 4 & 0 & 3 \end{bmatrix}$$

Find the new vector by dilating the original. **Graph** the transformed vector.

1. Dilate  $v = \langle 2, 3 \rangle$  by a factor of 2

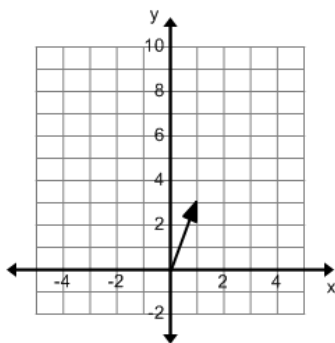


2. Dilate  $w = \langle 3, 9 \rangle$  by a factor of  $\frac{1}{3}$



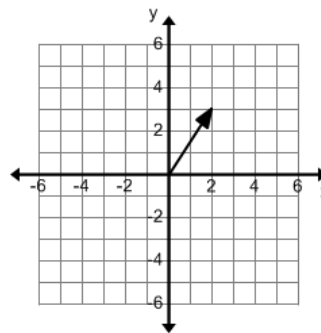
Find the new vector by rotating the original. **Graph** the transformed vector, the **describe** the results.

3. Rotate  $v = \langle 1, 3 \rangle$  using  $\begin{bmatrix} -3 & 0 \\ 0 & 3 \end{bmatrix}$



Description:

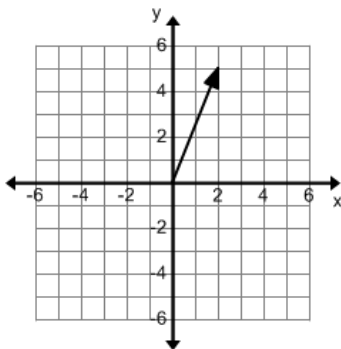
4. Rotate  $t = \langle 2, 3 \rangle$  using  $\begin{bmatrix} 2 & 0 \\ 0 & -2 \end{bmatrix}$



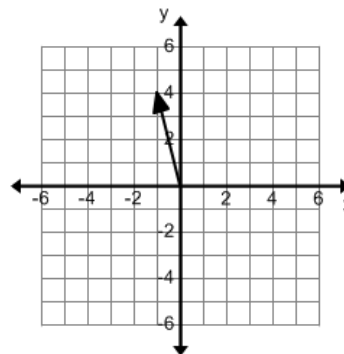
Description:

Find the new vector by reflecting the original.

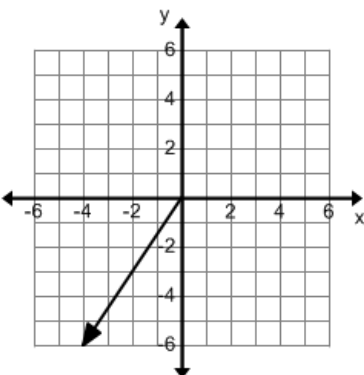
5. Reflect  $v = \langle 2, 5 \rangle$  across the origin



6. Reflect  $w = \langle -1, 4 \rangle$  across the x axis



7. Reflect  $t = \langle -4, -6 \rangle$  across the y axis



8. REVIEW:  
What is the component form for the vector with initial point  $(3, 7)$  and terminal point  $(-4, 3)$ ? What does this tell you about the vector?