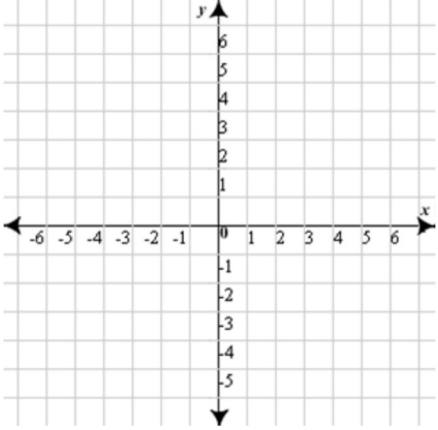
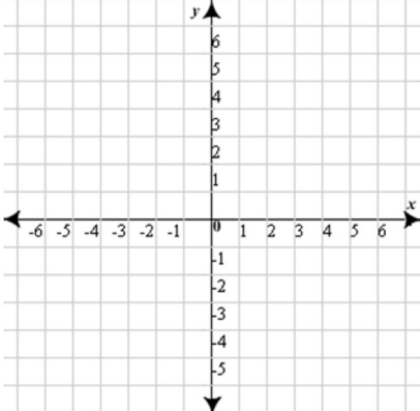


**Operations on Vectors 15.3**

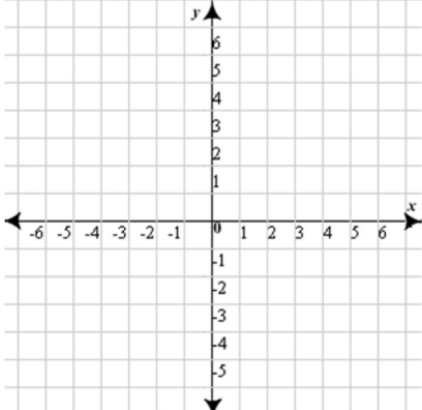
The sum of two vectors is called the \_\_\_\_\_.

<p><b>End to End method</b>  <math>\vec{u} = \langle 5,4 \rangle</math> and <math>\vec{v} = \langle 2,-9 \rangle</math>, find <math>\vec{u} + \vec{v}</math>.</p> <ol style="list-style-type: none"> <li>1. Position u and v so that the terminal point of u coincides with the initial point of v.</li> <li>2. The resultant vector, <math>u+v</math>, extends from the initial point of u to the terminal point of v.</li> </ol>	
<p><b>Component Wise method</b>  <math>\vec{u} = \langle 5,4 \rangle</math> and <math>\vec{v} = \langle 2,-9 \rangle</math>, find <math>\vec{u} + \vec{v}</math>.</p> <ol style="list-style-type: none"> <li>1. Add horizontal components</li> <li>2. Add vertical components</li> </ol>	
<p><b>Parallelogram method</b>  <math>\vec{u} = \langle 5,4 \rangle</math> and <math>\vec{v} = \langle 2,-9 \rangle</math>, find <math>\vec{u} + \vec{v}</math>.</p> <ol style="list-style-type: none"> <li>1. Draw both vectors starting at a common point, forming two sides of a parallelogram.</li> <li>2. Draw the other two sides.</li> <li>3. Draw in a new vector from the common starting point to the opposite vertex of the parallelogram.</li> </ol>	

**Magnitudes and Vector Addition**

<p>The magnitude of the sum of two vectors is not equal to the sum of the magnitudes of the two vectors <math>\ u + v\  \neq \ u\  + \ v\ </math>.</p>	<p><math>\vec{u} = \langle 5,4 \rangle</math> and <math>\vec{v} = \langle 2,-9 \rangle</math>, find</p> <p><math>\ u + v\  =</math></p> <p><math>\ u\  + \ v\  =</math></p>
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## Subtracting Vectors

<p>The difference of two vectors, <math>v-u</math>, is <math>v+(-u)</math>. <math>-u</math> is the opposite direction of <math>u</math>.</p>	
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## Multiply a vector by a scalar

We can stretch a vector by multiplying the vector by a scale factor. For example,  $2\vec{v}$  represents the vector that has the same direction as  $\vec{v}$ , but whose magnitude is twice that of  $\vec{v}$ .

If  $v = \langle 5, 4 \rangle$  find:  $6v$  and  $-3v$

## Scalar multiplication and magnitude

When multiplying a vector by a scalar the magnitude of  $kv$  ( $k$  is the scalar,  $v$  is the vector) is the magnitude of the vector times the absolute value of the scalar.

Find the magnitude of  $6v$  and  $-3v$